

~~2) $r(u, v) = (\sin(4u)\cos(v))i + (\sin(4u)\sin(v))j + (8u)k$~~

② $r(u, v) = (\sin(4u)\cos(v))i + (\sin(4u)\sin(v))j + (8u)k$

$$\int_D \int \int (r(u, v)) \underbrace{\left| \frac{dr}{du} \times \frac{dr}{dv} \right|}_{ds} du dv$$

$$\frac{dr}{du} = [4\cos v \cdot \cos 4u, 4\sin v \cdot \cos 4u, 8]$$

$$\frac{dr}{dv} = [-\sin 4u \cdot \sin v, \sin 4u \cdot \cos v, 0]$$

$$\frac{dr}{du} \times \frac{dr}{dv} = \begin{vmatrix} i & j & k \\ 4\cos v \cdot \cos 4u & 4\sin v \cdot \cos 4u & 8 \\ -\sin 4u \cdot \sin v & \sin 4u \cdot \cos v & 0 \end{vmatrix}$$

$$= i(-8\sin 4u \cdot \cos v) - j(8\sin 4u \cdot \sin v)$$

$$+ k(2\sin 8u)$$

$$= [-8\sin 4u \cdot \cos v, -8\sin 4u \cdot \sin v, 2\sin 8u]$$

$$= \left| \frac{dr}{du} \times \frac{dr}{dv} \right| = \sqrt{(-8\sin 4u \cdot \cos v)^2 + (-8\sin 4u \cdot \sin v)^2 + (2\sin 8u)^2}$$

$$= \left| \frac{dr}{du} \times \frac{dr}{dv} \right| = 2 \sqrt{\sin^2 8u + 16 \sin^2 4u}$$

$$= \int_0^{\frac{\pi}{2}} \int_0^{\pi} 2 \sqrt{\sin^2 8u + 16 \sin^2 4u} \cdot \sqrt{8^2 + 4^2 \cos^2 4u} dv du$$

$$= \frac{52}{3} \pi$$